

Key

Objective: Use dimensional analysis to convert from one rate to another.What is a Rate? *a ratio with two different units*Examples: $\frac{\text{miles}}{\text{hour}}$ $\frac{\text{cents}}{\text{ounce}}$

Write some other rates and share with your neighbor:

*\$/hour mi/gal.***Example:** Convert 38 feet/second into miles per hour

1. Write the rate given as a ratio

$$\frac{38 \text{ feet}}{1 \text{ second}}$$

2. Convert the units of the numerator (if needed)

$$\frac{38 \cancel{\text{ feet}}}{1 \text{ second}} \cdot \frac{1 \text{ mile}}{5280 \cancel{\text{ feet}}}$$

3. Convert the units of the denominator (if needed)

$$\frac{38 \cancel{\text{ feet}}}{1 \cancel{\text{ second}}} \cdot \frac{1 \text{ mile}}{5280 \cancel{\text{ feet}}} \cdot \frac{3600 \cancel{\text{ seconds}}}{1 \text{ hour}}$$

4. Cancel dimensions

5. Multiply all numerators then all denominators

$$\frac{136,800 \text{ miles}}{5280 \text{ hours}}$$

6. Divide numerator by denominator to create a "unit rate"

$$25.91 \frac{\text{miles}}{\text{hour}} \quad \text{or} \quad 25.91 \text{ miles per hour}$$

DON'T FORGET TO LABEL YOUR ANSWER

or 25.91 miles/hour

Practice:

1. 55 km/hr to mi/hr

$$\frac{55 \text{ km}}{1 \text{ hr.}} \cdot \frac{1 \text{ mi}}{1.6 \text{ km}} = \frac{55}{1.6} = 34.375$$

34.4 mi/hr.

2. 19 quarts/min to cups/min

$$\frac{19 \text{ qts.}}{1 \text{ min}} \cdot \frac{2 \text{ pints}}{1 \text{ qt.}} \cdot \frac{2 \text{ cups}}{1 \text{ pint}} = 76 \text{ cups/min}$$

3. 1.5 yards/min to in/sec

$$\frac{1.5 \text{ yards}}{1 \text{ min}} \cdot \frac{1 \text{ min}}{60 \text{ sec}} \cdot \frac{3 \text{ ft.}}{1 \text{ yd}} \cdot \frac{12 \text{ in}}{1 \text{ ft.}} = \frac{54}{60} = 0.9 \text{ in/sec}$$

4. 25 km/L to mi/gal

$$\frac{25 \text{ km}}{1 \text{ L}} \cdot \frac{1 \text{ mi}}{1.6 \text{ km}} \cdot \frac{3.8 \text{ L}}{1 \text{ gal}} = \frac{95}{1.6} = 59.375$$

59.4 mi/gal

5. 75 mi/hr to ft/sec

$$\frac{75 \text{ mi}}{1 \text{ hr.}} \cdot \frac{5280 \text{ ft.}}{1 \text{ mi}} \cdot \frac{1 \text{ hr}}{3600 \text{ sec}} = \frac{396000}{3600} = 110 \text{ ft./sec}$$

6. 320 ft/min to yds/hr

$$\frac{320 \text{ ft.}}{1 \text{ min}} \cdot \frac{60 \text{ min}}{1 \text{ hr}} \cdot \frac{1 \text{ yard}}{3 \text{ ft.}} = \frac{19200}{3} = 6400 \text{ yds./hr.}$$

7. 12 fl. oz./day to gal/year

$$\frac{12 \text{ fl. oz.}}{1 \text{ day}} \cdot \frac{365 \text{ day}}{1 \text{ year}} \cdot \frac{1 \text{ gal}}{128 \text{ fl. oz.}} = \frac{4380}{128} = 34.21875$$

34.2 gal/yr.