## Unit 2 3.5

## Objective: Use a system of inequalities to solve a problem in context.

In order to raise money, you are planning to work during the summer babysitting and cleaning houses. You earn \$10 per hour while babysitting and \$20 per hour while cleaning houses. You need to earn at least \$1000 during the summer.

- 1. Write an **expression** to represent the amount of money earned while babysitting. Be sure to choose a variable to represent the number of hours spent babysitting.
- 2. Write an **expression** to represent the amount of money earned while cleaning houses.
- 3. Write a mathematical model (inequality) representing the total amount of money earned over the summer from babysitting and cleaning houses.
- 4. Graph the inequality. Graph the hours babysitting on the x-axis and the hours cleaning houses on the y-axis.

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- 5. Use the graph to answer the following questions:
  - a. Why does the graph only fall in the 1<sup>st</sup> quadrant?
  - b. Is it acceptable to earn exactly \$1000?
  - c. What are some possible combinations of outcomes that total more than \$1000?
  - d. Where do all of these outcomes fall on the graph?
- e. Is it acceptable to work 10 hours babysitting and 10 hours cleaning houses?
  - i. Why or why not?
- f. Where does the combination of 10 hours babysitting and 10 hours cleaning houses fall on the graph?
- g. Are combinations that fall in this area a solution?
  - i. Why or why not?

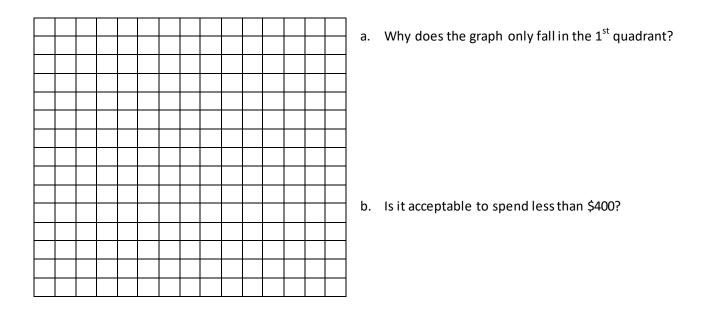
- 6. How would the model change if you could only earn more than \$1000? Write a new model to represent needing to earn more than \$1000.
  - a. How would this change the graph of the model?

b. Would the line still be part of the solution?

c. How would you change the line to show this?

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- 7. You plan to use part of the money you earned from your summer job to buy jeans and shirts for school. Jeans cost \$40 per pair and shirts are \$20 each. You want to spend less than \$400 of your money on these items.
  - a. Write an inequality representing the amount of money spent on jeans and shirts.
  - b. Graph the inequality. Graph the number of jeans on the x-axis and shirts on the y-axis.



c. What are some possible combinations of outcomes that total less than \$400?

f. Is it acceptable to spend exactly \$400? How does the graph show this?

g. Is it acceptable to spend more than \$400? Where do all of the combinations that total more than \$400 fall?

- 8. Explain the difference between a solid line and a dashed line when graphing inequalities.
  - a. How can you determine from the inequality whether or not the line will be solid or dashed?
  - b. How can you look at the graph and know if the line is part of the solution?
- 9. How do you determine which area of the graph of an inequality to shade?
  - a. What is special about the shaded area of an inequality?

b. What is special about the area that is not shaded?

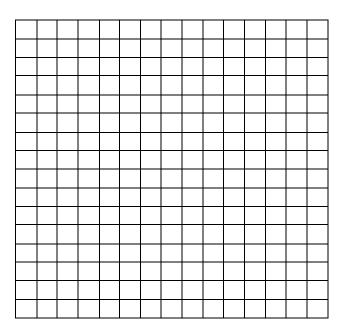
- 10. A store sells two types of toys, zingers and zappers. The store owner pays \$8 for each zinger and \$14 for each zapper. The store owner estimates that no more than 2000 toys will be sold every month. Additionally, she plans to spend less than \$20,000 on the toys.
  - a. What are we trying to find?
  - b. What variables will be used, and what do they represent?
  - c. What information is given?
  - d. Write a system of inequalities to represent the situation.

e. Graph the system.

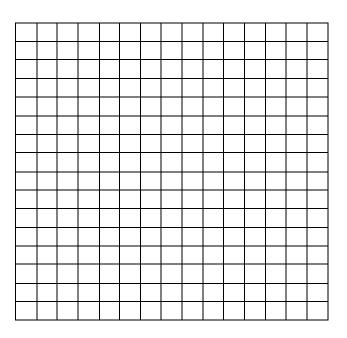
f. List 3 ordered pairs that are solutions to the system.

g. List one ordered pair that is on a line, but not part of the solution.

h. List one ordered pair that is on a line, and part of the solution.



- 11. Suppose a car dealer makes a profit of \$500 for each mid-sized car sold and \$750 for each SUV sold. The dealer must sell at least two mid-sized car for each SUV sold. They also want to make at least \$3500 in profit each week.
  - a. Graph the scenario.



- b. Suppose the dealer sells 2 SUVs. How many mid-size cars must be sold to reach the profit goal of at least \$3500?
- c. If the dealer sells only one SUV, how many mid-size cars must be sold to meet the goal?
- d. How many SUVs need to be sold to meet the goal if 5 mid-size cars are sold?

## CHALLENGE:

12. Use the scenario from #10. If the store owner can spend up to \$20,000 (not just less than), and she makes \$2 profit on every zinger and \$3 profit on every zapper, how many of each type of toy should be purchased in order to maximize her monthly total profit?