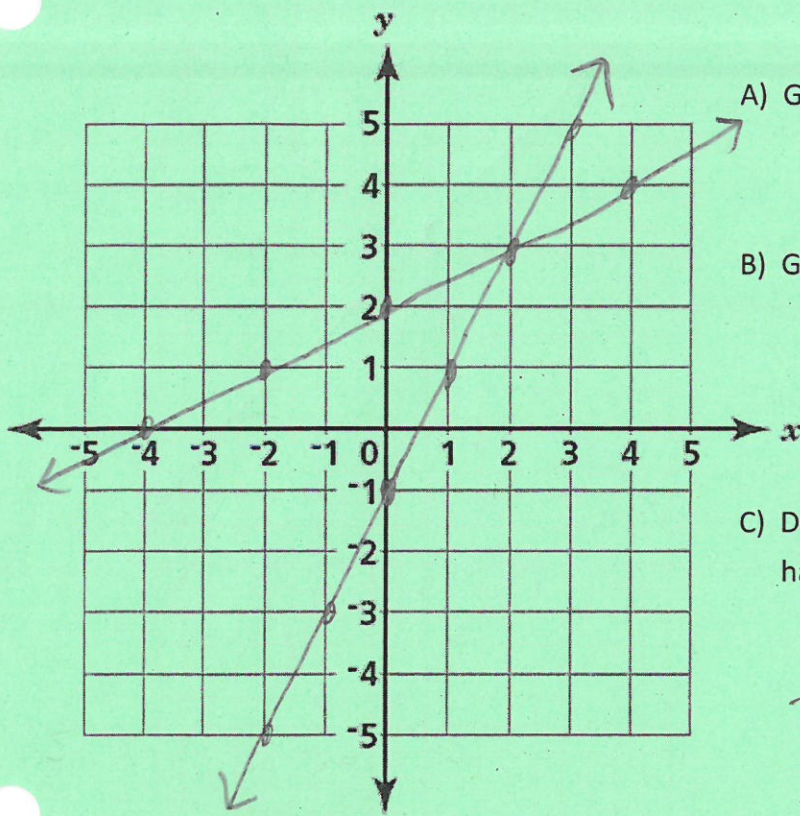


Systems of Equations: Solve by Graphing



A) Graph the equation $y = 2x - 1$ on the grid.

B) Graph the equation $y = \frac{1}{2}x + 2$ on the same grid.

C) Do the equations $y = 2x - 1$ and $y = \frac{1}{2}x + 2$ have any solutions in common? How do you know?

yes, the point (2, 3)

$$\begin{array}{l} 3 = 2(2) - 1 \\ 3 = 3 \end{array} \quad \left\{ \begin{array}{l} 3 = \frac{1}{2}(2) + 2 \\ 3 = 3 \end{array} \right.$$

A set of two or more equations is called a **system of equations**. A solution of a system is an **ordered pair** that satisfies both equations.

Examples:

1. Which ordered pair(s) is/are a solution(s) to $-8x + 6y = 12$?

- a. (6, -10) b. (0, 2) c. (-9, -10) d. (14, 9)

2. Which ordered pair(s) is/are a solution(s) to $4x - 5y = 30$?

- a. (20, 10) b. (10, -14) c. (2, 2) d. (-6, 0)

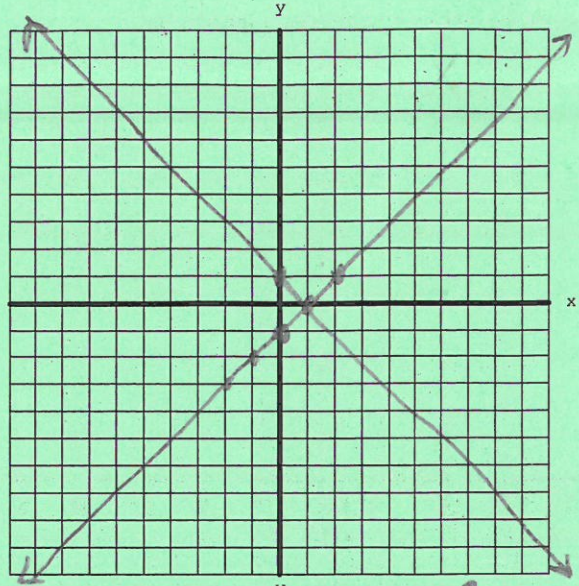
3. Which ordered pair(s) is/are a solution(s) to $4x - y = 9$?

- a. (-10, 9) b. (2, -1) c. (-5, -2) d. (7, 22)

Problem Set 1: Use the graph to determine the solution to the system of equations

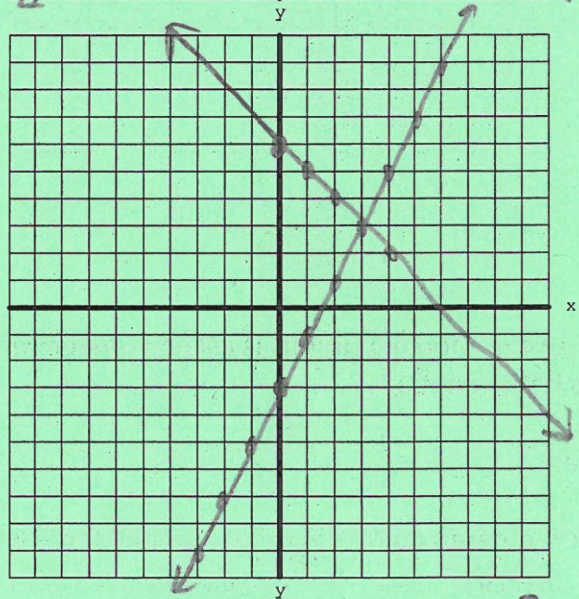
A.
$$\begin{cases} y = x - 1 \\ y = -x + 1 \end{cases}$$

(1, 0)



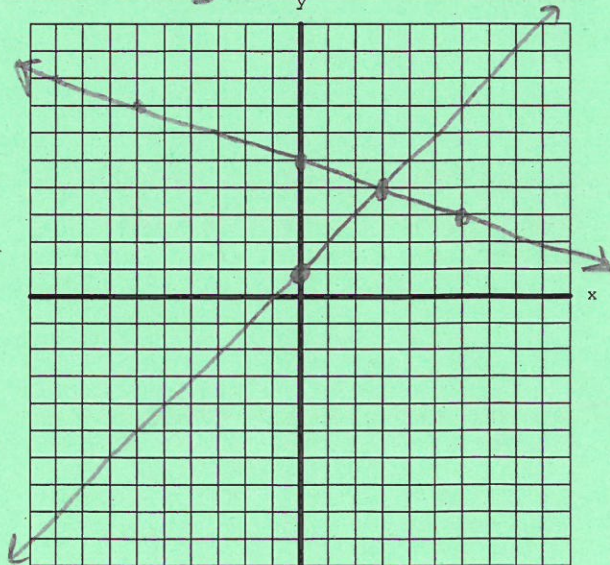
B.
$$\begin{cases} y = 2x - 3 \\ y = -x + 6 \end{cases}$$

(3, 3)



C.
$$\begin{cases} y = x + 1 \\ y = -\frac{1}{3}x + 5 \end{cases}$$

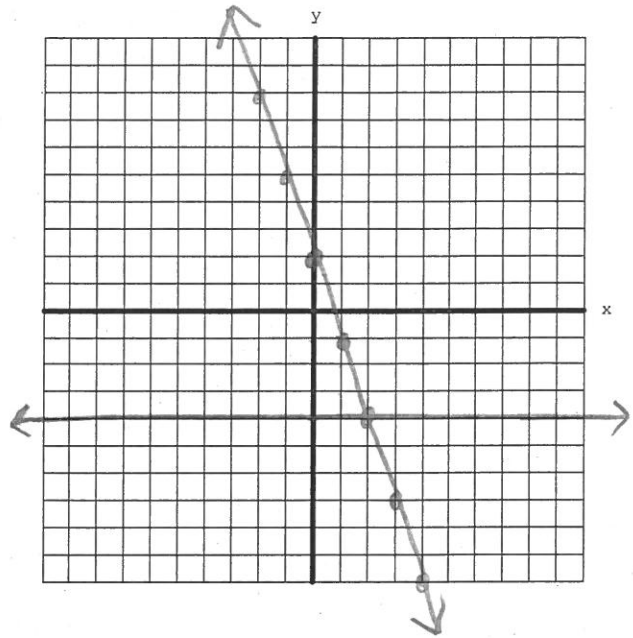
(3, 4)



Problem Set 2: Graph each system of equations to determine the solution.

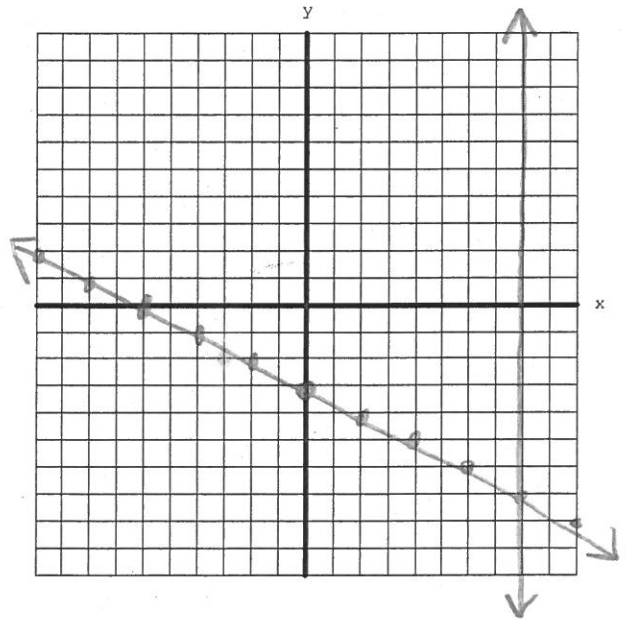
A. $\begin{cases} y = 2x - 4 \\ y = -3x + 2 \end{cases}$

$(2, -4)$



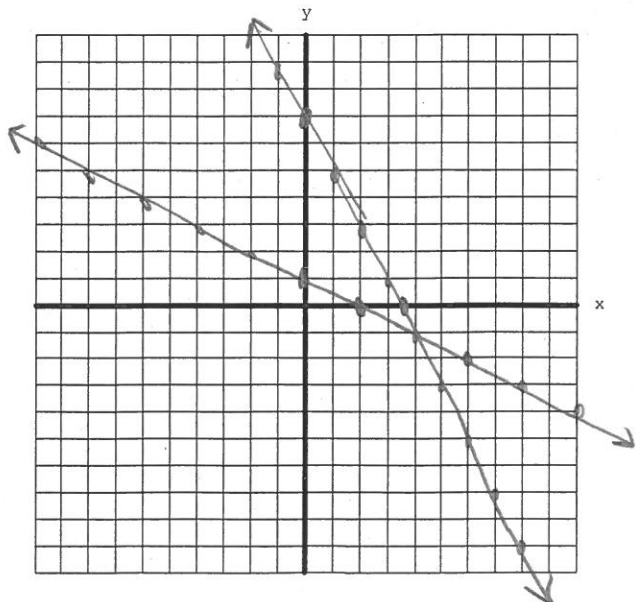
B. $\begin{cases} y = \frac{1}{2}x + 1 & x = 8 \\ 2x + 4y = -12 \end{cases}$

$(8, -7)$



C. $\begin{cases} 2x + y = 7 \\ x + 2y = 2 \end{cases}$

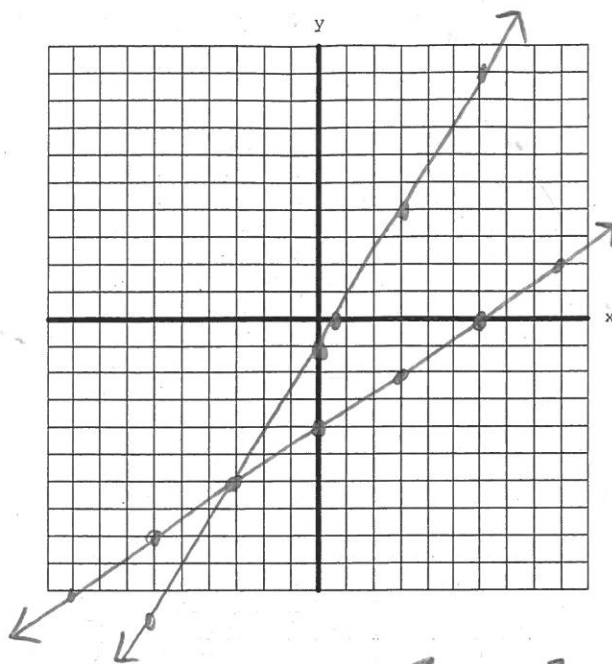
$(4, -1)$



Problem Set 3: Graph each system of equations to determine the solution.

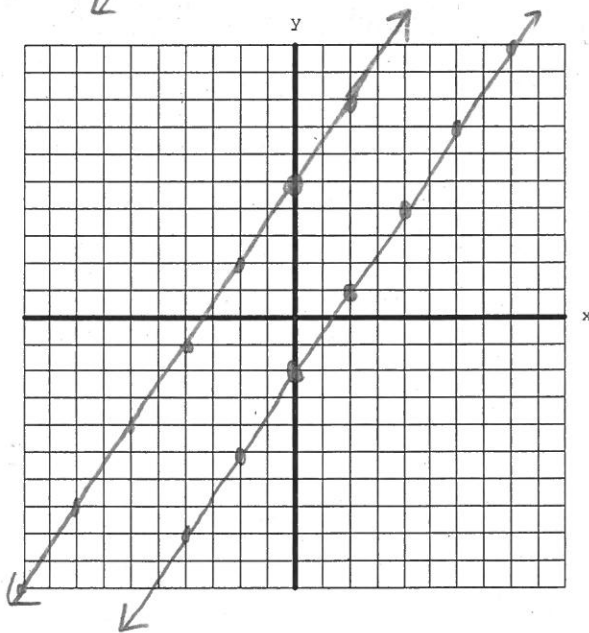
A. $\begin{cases} 2x - 3y = 12 \\ 10x - 6y = 6 \end{cases}$

$(-3, -6)$



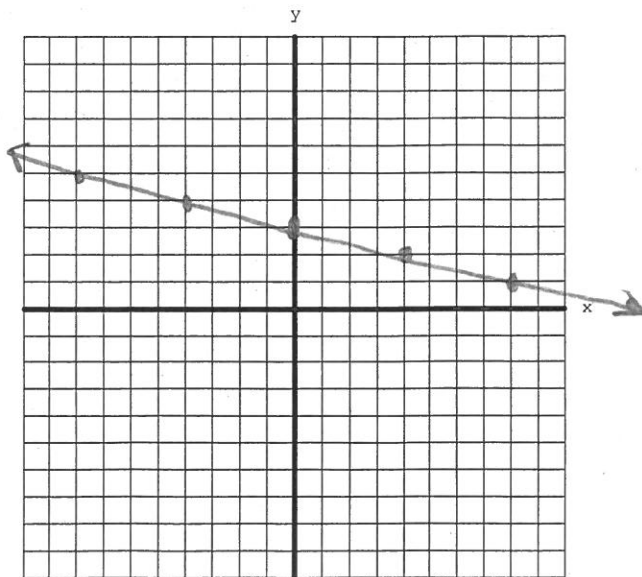
B. $\begin{cases} y = \frac{3}{2}x + 5 \\ y = \frac{3}{2}x - 2 \end{cases}$

no solution



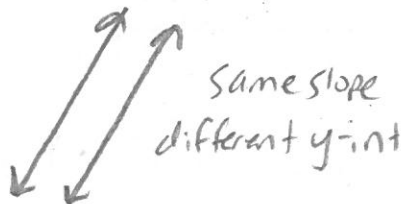
C. $\begin{cases} x + 4y = 12 \\ y = -\frac{1}{4}x + 3 \end{cases}$ > same line

infinite solutions

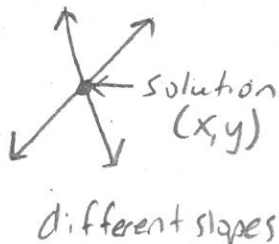


A system of two linear equations can have no, one, or an infinite number of solutions:

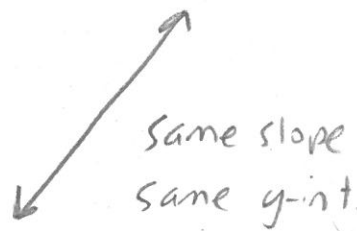
No Solution: parallel lines



One Solution: intersecting lines



Infinite Solutions: same lines



Consider the equation $y = 5x - 3$. Write a second equation that would create a system with...

A) zero solutions

$$y = 5x + 2$$

$$m = 5 \quad b \neq -3$$

B) one solution

$$y = \frac{5}{2}x - 3$$

$$m \neq 5$$

C) infinite solutions

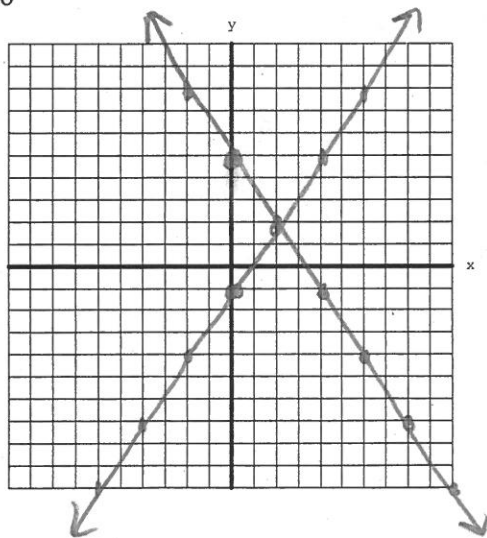
$$2y = 10x - 6$$

another version of
the same line

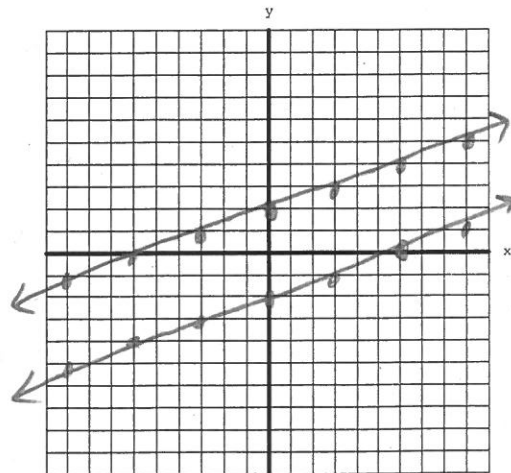
Extra Practice

1.
$$\begin{cases} y = \frac{3}{2}x - 1 \\ 3x + 2y = 10 \end{cases}$$

$(2, 2)$

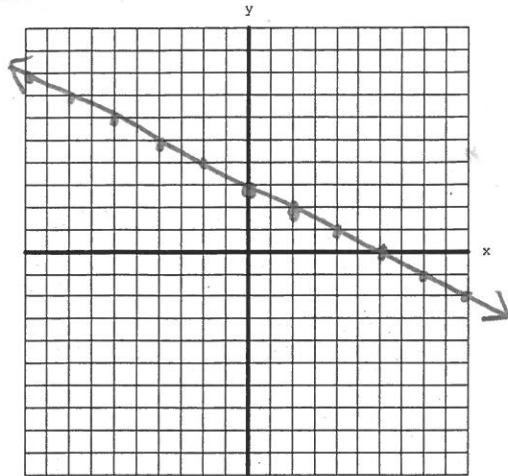


2.
$$\begin{cases} y = \frac{1}{3}x + 2 \\ 2x - 6y = 12 \end{cases}$$



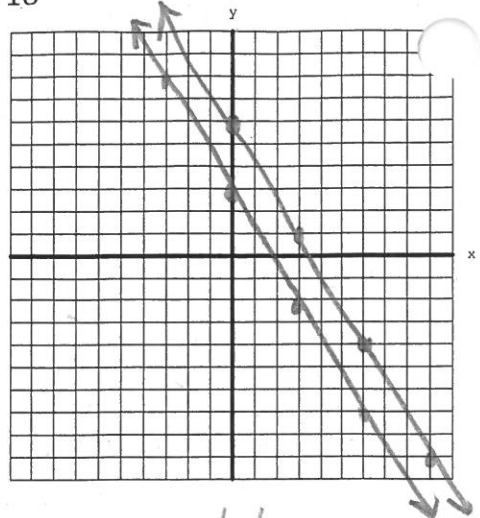
no solution

3. $\begin{cases} y = -\frac{1}{2}x + 3 \\ 2x + 4y = 12 \end{cases}$ *> same line*



Infinite Solutions

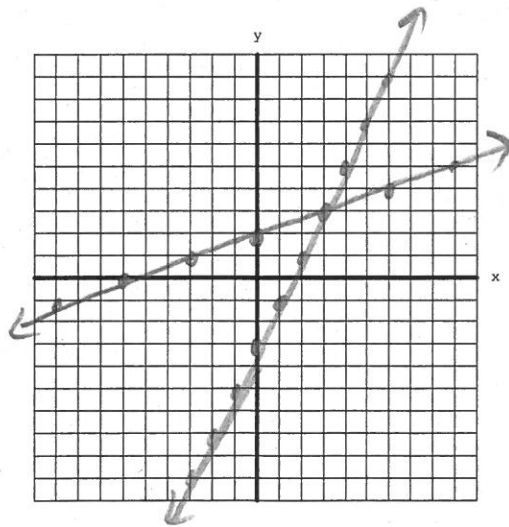
4. $\begin{cases} y = -\frac{5}{3}x + 6 \\ 10x + 6y = 18 \end{cases}$



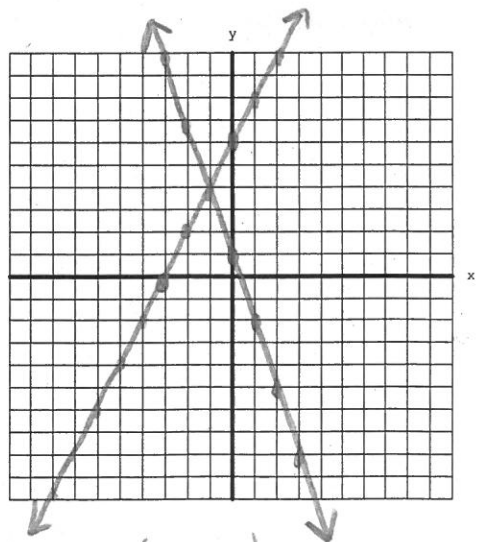
No solution

5. $\begin{cases} y = \frac{1}{3}x + 2 \\ -2x + y = -3 \end{cases}$

(3, 3)



6. $\begin{cases} y = -3x + 1 \\ 2x - y = -6 \end{cases}$



(-1, 4)